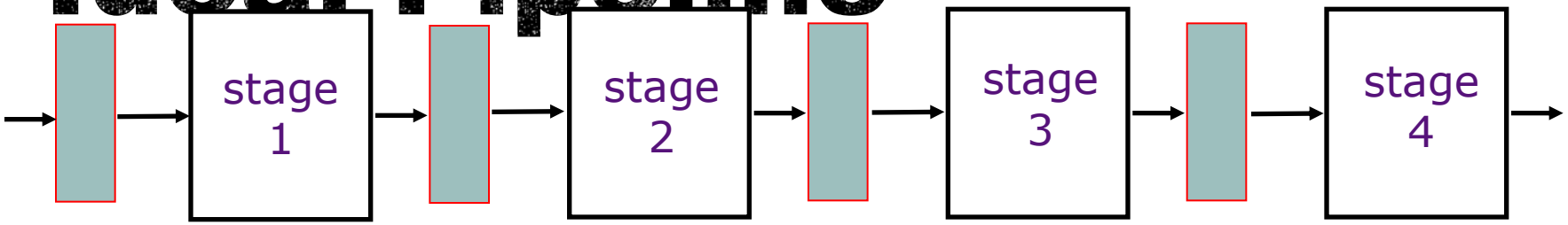
Architecture of Computer Systems
Lecture 4 - Pipelining

Last time in Lecture 3

- Microcoding became less attractive as gap between RAM and ROM speeds reduced
- Complex instruction sets difficult to pipeline, so difficult to increase performance as gate count grew
- Load-Store RISC ISAs designed for efficient pipelined implementations
  - Very similar to vertical microcode
  - Inspired by earlier Cray machines (more on these later)
- Iron Law explains architecture design space
  - Trade instructions/program, cycles/instruction, and time/cycle

An Ideal Pipeline



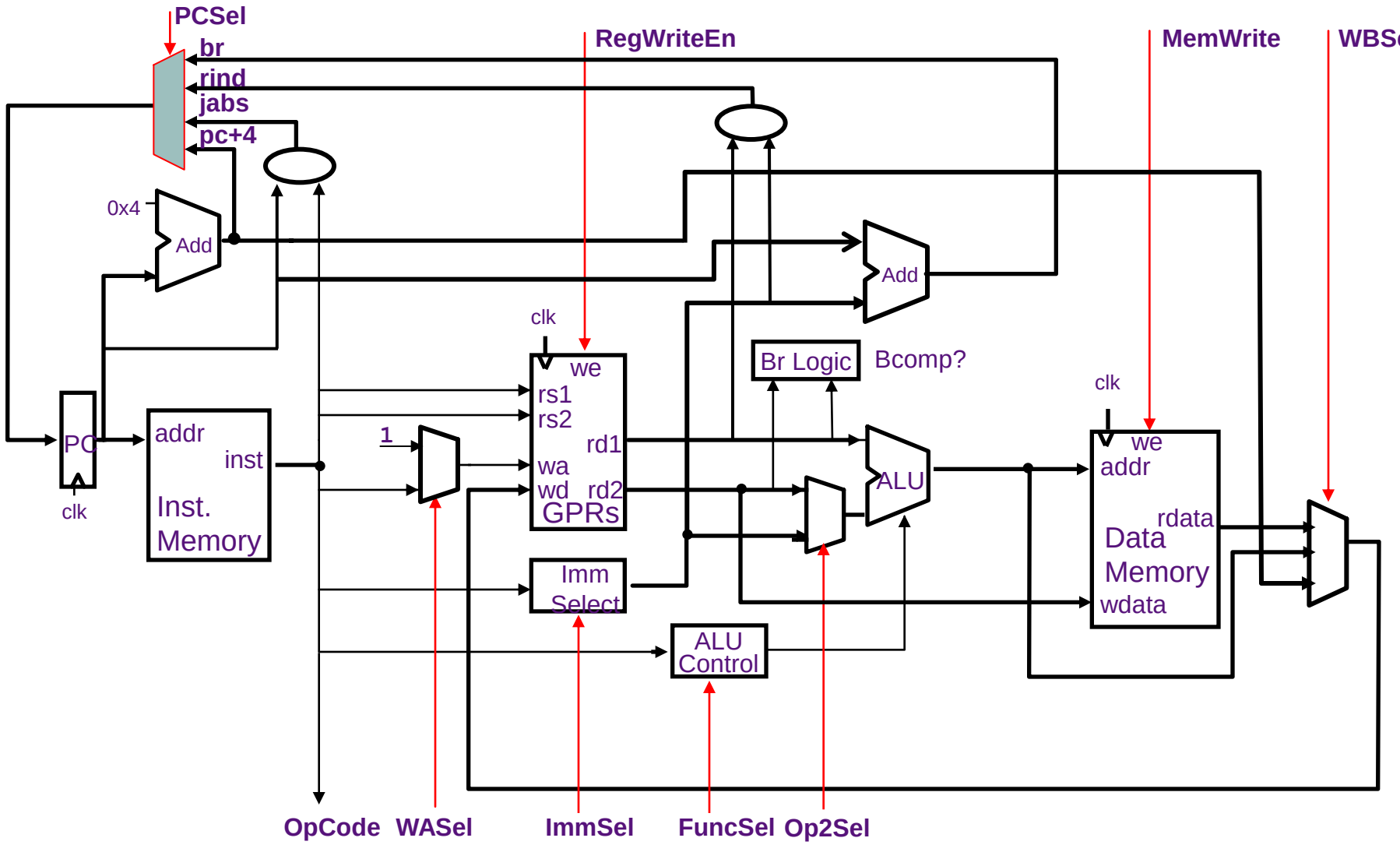
- All objects go through the same stages
- No sharing of resources between any two stages
- Propagation delay through all pipeline stages is equal
- The scheduling of an object entering the pipeline is not affected by the objects in other stages

These conditions generally hold for industrial assembly lines, but instructions depend on each other!

Pipelined RISC-V

- To pipeline RISC-V:
- First build RISC-V without pipelining with CPI=1
- Next, add pipeline registers to reduce cycle time while maintaining CPI=1

Lecture 3: Unpipelined Datapath for RISC-V

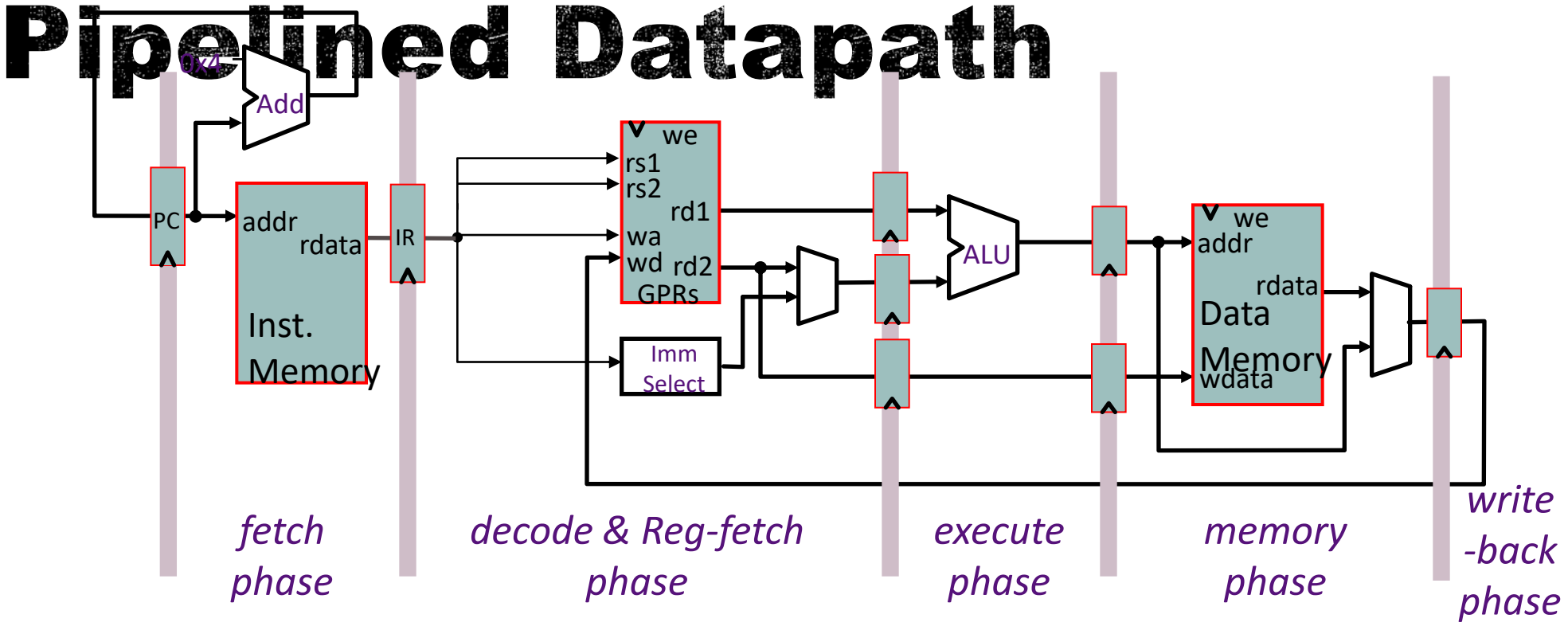


Lecture 3: Hardwired Control Table

Opcode	ImmSel	Op2Sel	FuncSel	MemWr	RFWen	WBSel	WASel	PCSel
ALU	*	Reg	Func	no	yes	ALU	rd	pc+4
ALUi	$IType_{12}$	Imm	Op	no	yes	ALU	rd	pc+4
LW	$IType_{12}$	Imm	+	no	yes	Mem	rd	pc+4
SW	$BsType_{12}$	Imm	+	yes	no	*	*	pc+4
BEQ_{true}	$BrType_{12}$	*	*	no	no	*	*	br
BEQ_{false}	$BrType_{12}$	*	*	no	no	*	*	pc+4
J	*	*	*	no	no	*	*	jabs
JAL	*	*	*	no	yes	PC	X1	jabs
JALR	*	*	*	no	yes	PC	rd	rind

Op2Sel= Reg / Imm WBSel = ALU / Mem / PC
WASel = rd / X1 PCSel = pc+4 / br / rind / jabs

Pipelined Datapath



Clock period can be reduced by dividing the execution of an instruction into multiple cycles

$t_C > \max \{t_{IM}, t_{RF}, t_{ALU}, t_{DM}, t_{RW}\}$ (= t_{DM} *probably*)

However, CPI will increase unless instructions are pipelined

"Iron Law" of Processor Performance

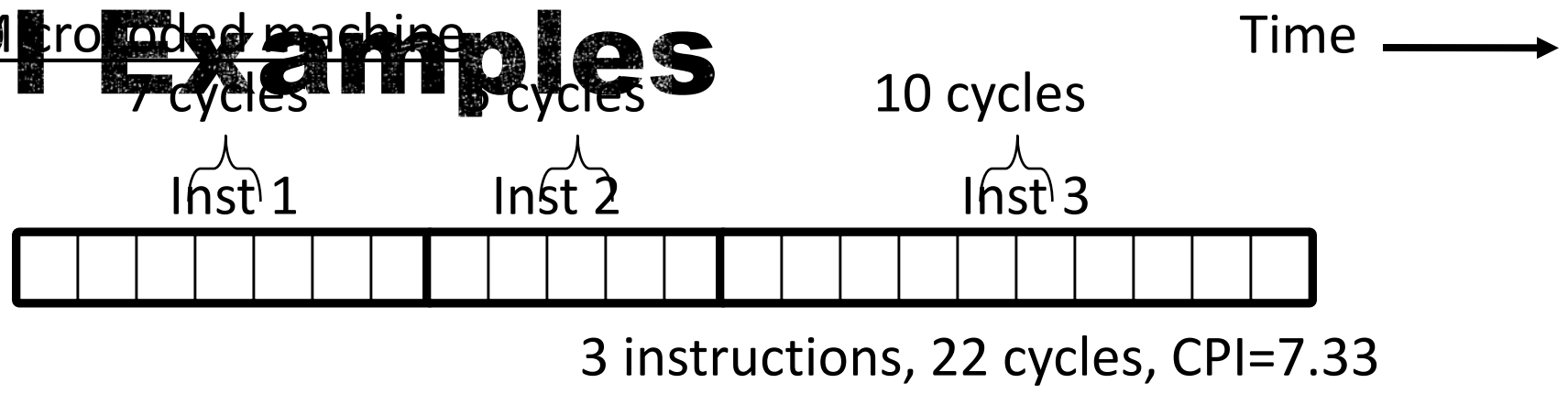
$$\frac{\text{Time}}{\text{Program}} = \frac{\text{Instructions}}{\text{Program}} * \frac{\text{Cycles}}{\text{Instruction}} * \frac{\text{Time}}{\text{Cycle}}$$

- Instructions per program depends on source code, compiler technology, and ISA
- Cycles per instructions (CPI) depends on ISA and μarchitecture
- Time per cycle depends upon the μarchitecture and base technology

	Microarchitecture	CPI	cycle time
Lecture 2	Microcoded	>1	short
Lecture 3	Single-cycle unpipelined	1	long
Lecture 4	Pipelined	1	short

CPI Examples

Microcoded machine

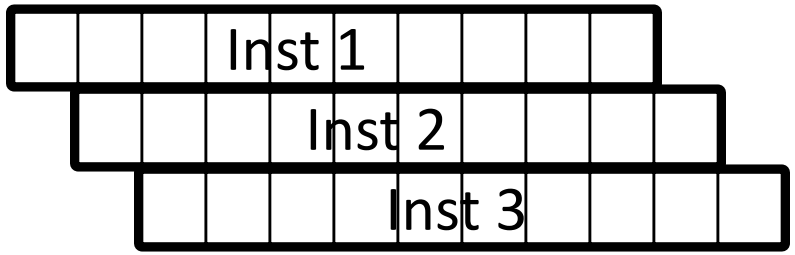


3 instructions, 22 cycles, CPI=7.33

Unpipelined machine

3 instructions, 3 cycles, CPI=1

Pipelined machine



3 instructions, 3 cycles, CPI=1

5-stage pipeline CPI≠5!!!

Technology Assumptions

- A small amount of very fast memory (caches) backed up by a large, slower memory
- Fast ALU (at least for integers)
- Multiported Register files (slower!)

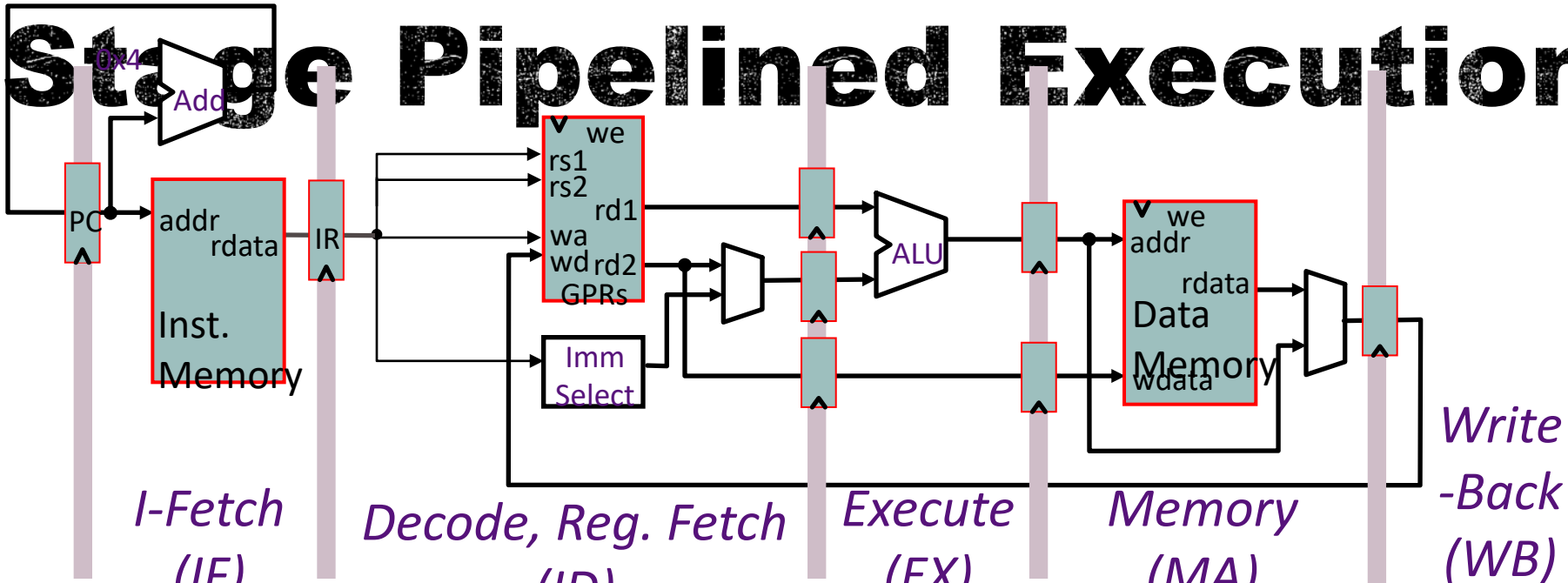
Thus, the following timing assumption is reasonable

$$t_{IM} \approx t_{RF} \approx t_{ALU} \approx t_{DM} \approx t_{RW}$$

A 5-stage pipeline will be focus of our detailed design

- some commercial designs have over 30 pipeline stages to do an integer add!

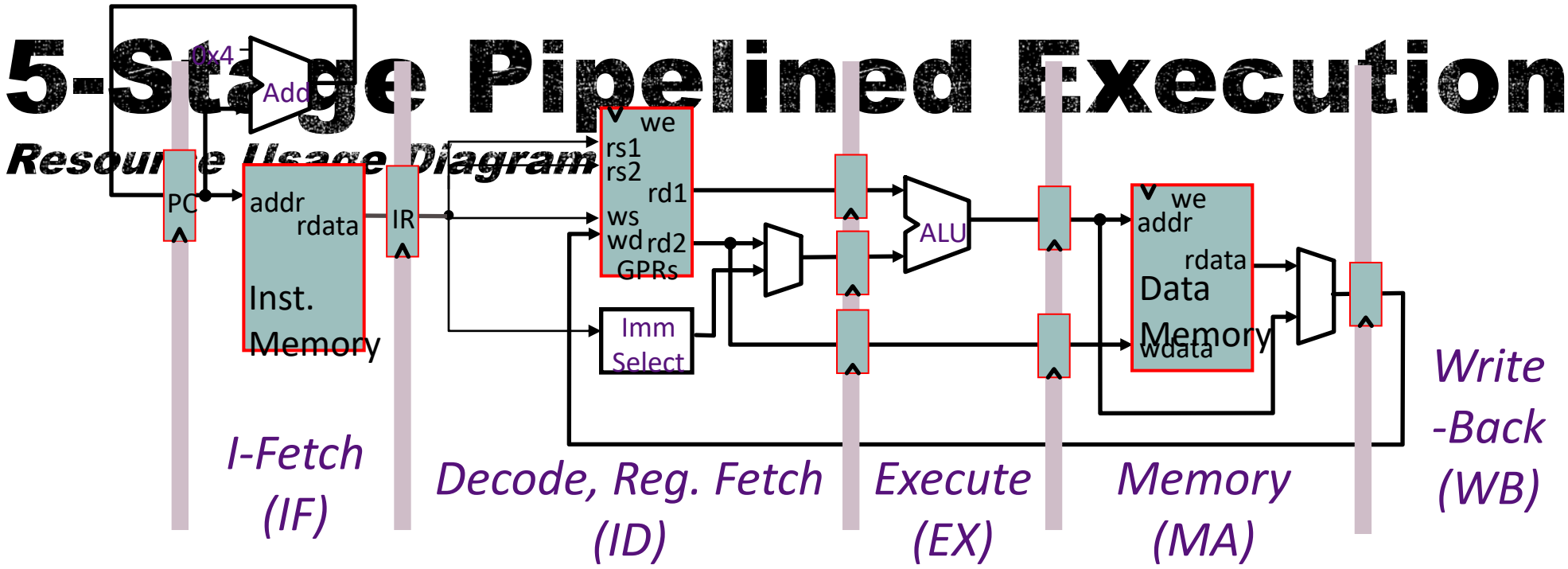
5-Stage Pipelined Execution



time	t0	t1	t2	t3	t4	t5	t6	t7	. . . .
instruction1	IF_1	ID_1	EX_1	MA_1	WB_1				
instruction2		IF_2	ID_2	EX_2	MA_2	WB_2			
instruction3			IF_3	ID_3	EX_3	MA_3	WB_3		
instruction4				IF_4	ID_4	EX_4	MA_4	WB_4	
instruction5					IF_5	ID_5	EX_5	MA_5	WB_5

5-Stage Pipelined Execution

Resource Usage Diagram

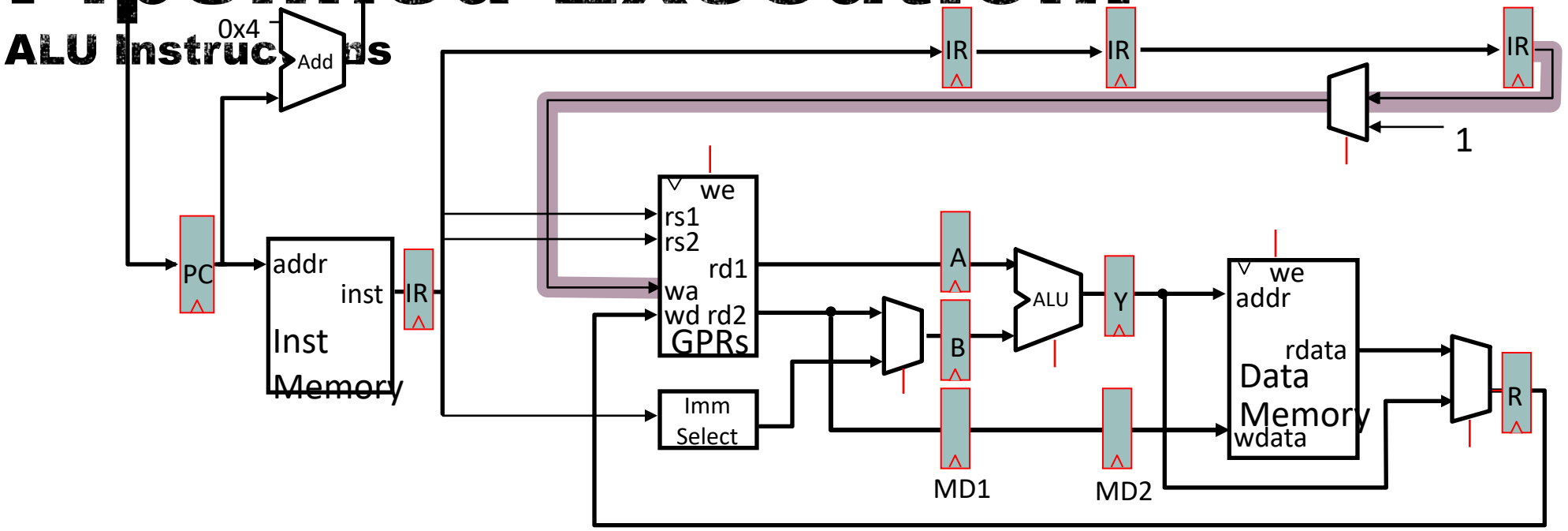


Resources

time	t0	t1	t2	t3	t4	t5	t6	t7	. . . .
IF	I_1	I_2	I_3	I_4	I_5				
ID		I_1	I_2	I_3	I_4	I_5			
EX			I_1	I_2	I_3	I_4	I_5		
MA				I_1	I_2	I_3	I_4	I_5	
WB					I_1	I_2	I_3	I_4	I_5

Pipelined Execution:

ALU Instructions

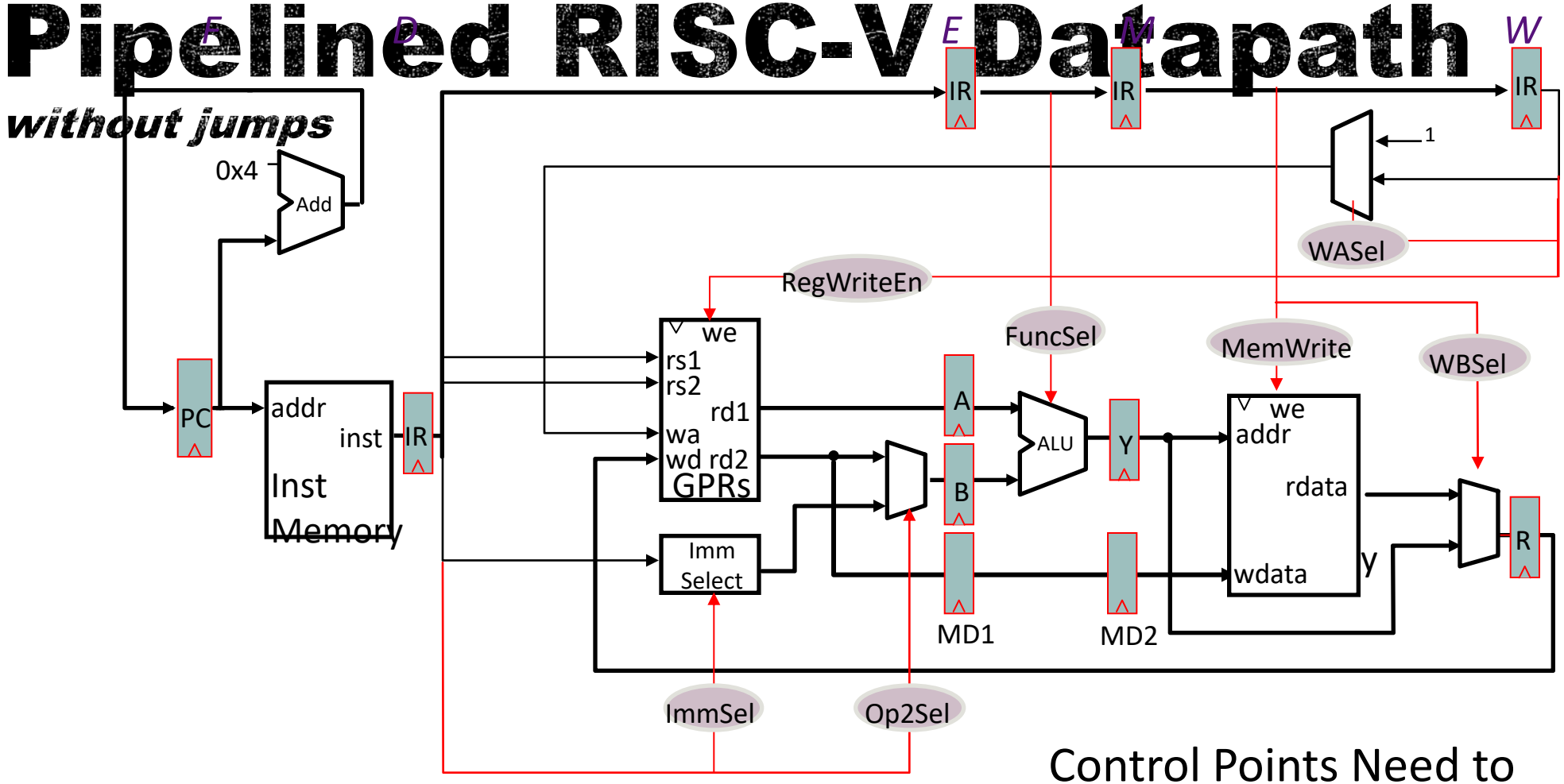


Not quite correct!

We need an Instruction Reg (IR) for each stage

Pipelined RISC-V Datapath

without jumps



Control Points Need to Be Connected

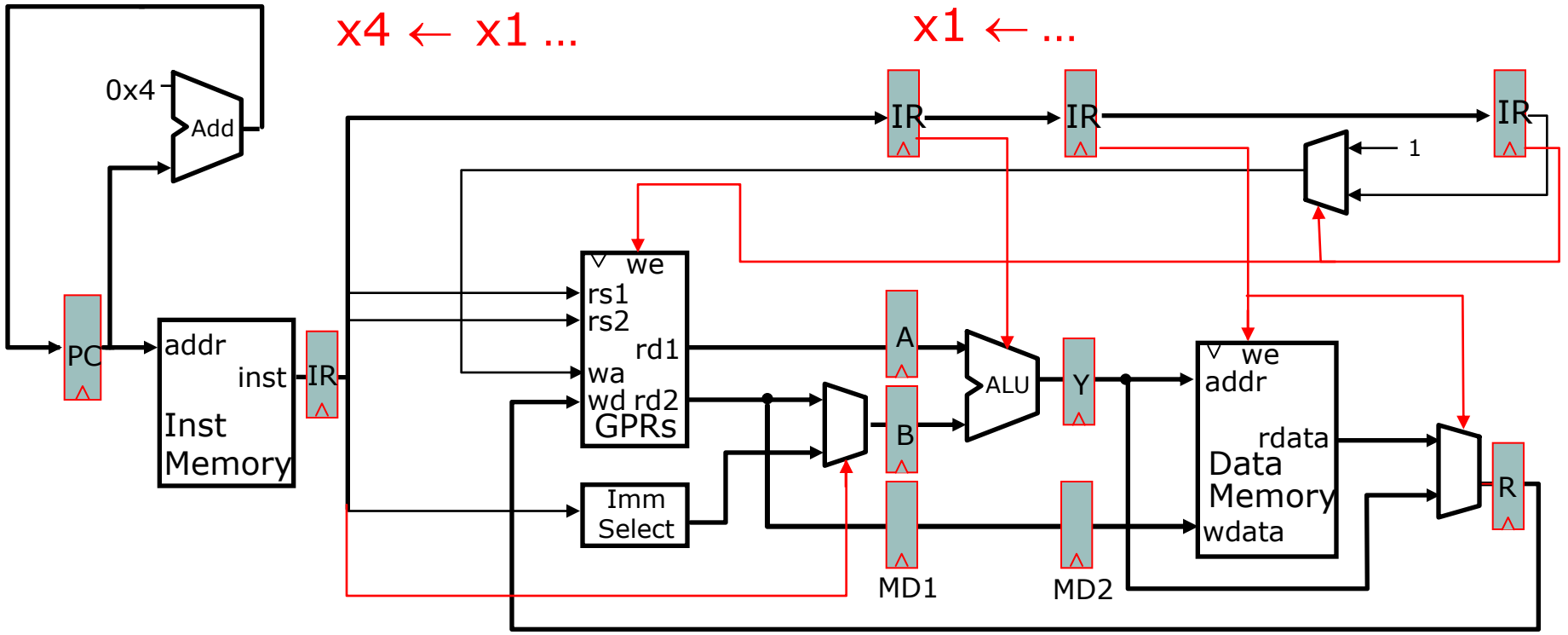
Instructions interact with each other in pipeline

- An instruction in the pipeline may need a resource being used by another instruction in the pipeline → *structural hazard*
- An instruction may depend on something produced by an earlier instruction
  - Dependence may be for a data value
    → *data hazard*
  - Dependence may be for the next instruction's address
    → *control hazard (branches, exceptions)*

Resolving Structural Hazards

- Structural hazard occurs when two instructions need same hardware resource at same time
  - Can resolve in hardware by stalling newer instruction till older instruction finished with resource
- A structural hazard can always be avoided by adding more hardware to design
  - E.g., if two instructions both need a port to memory at same time, could avoid hazard by adding second port to memory
- Our 5-stage pipeline has no structural hazards by design
  - Thanks to RISC-V ISA, which was designed for pipelining

Data Hazards



…
x1 ← x0 + 10
x4 ← x1 + 17
…

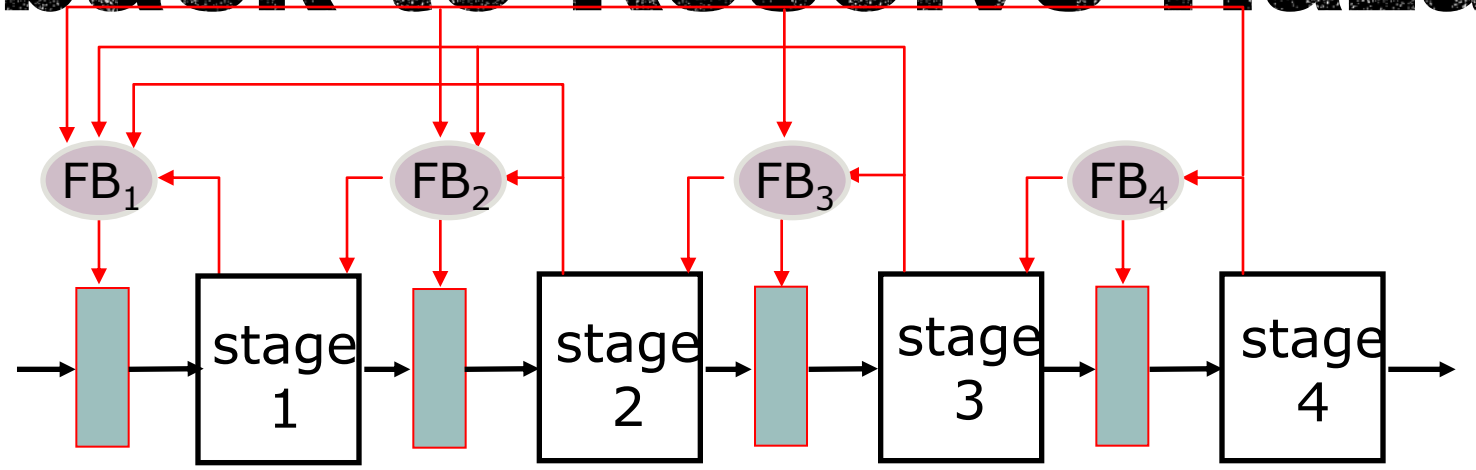
x1 is stale. Oops!

Resolving Data Hazards (1)

Strategy 1:

Wait for the result to be available by freezing earlier pipeline stages ➔ interlocks

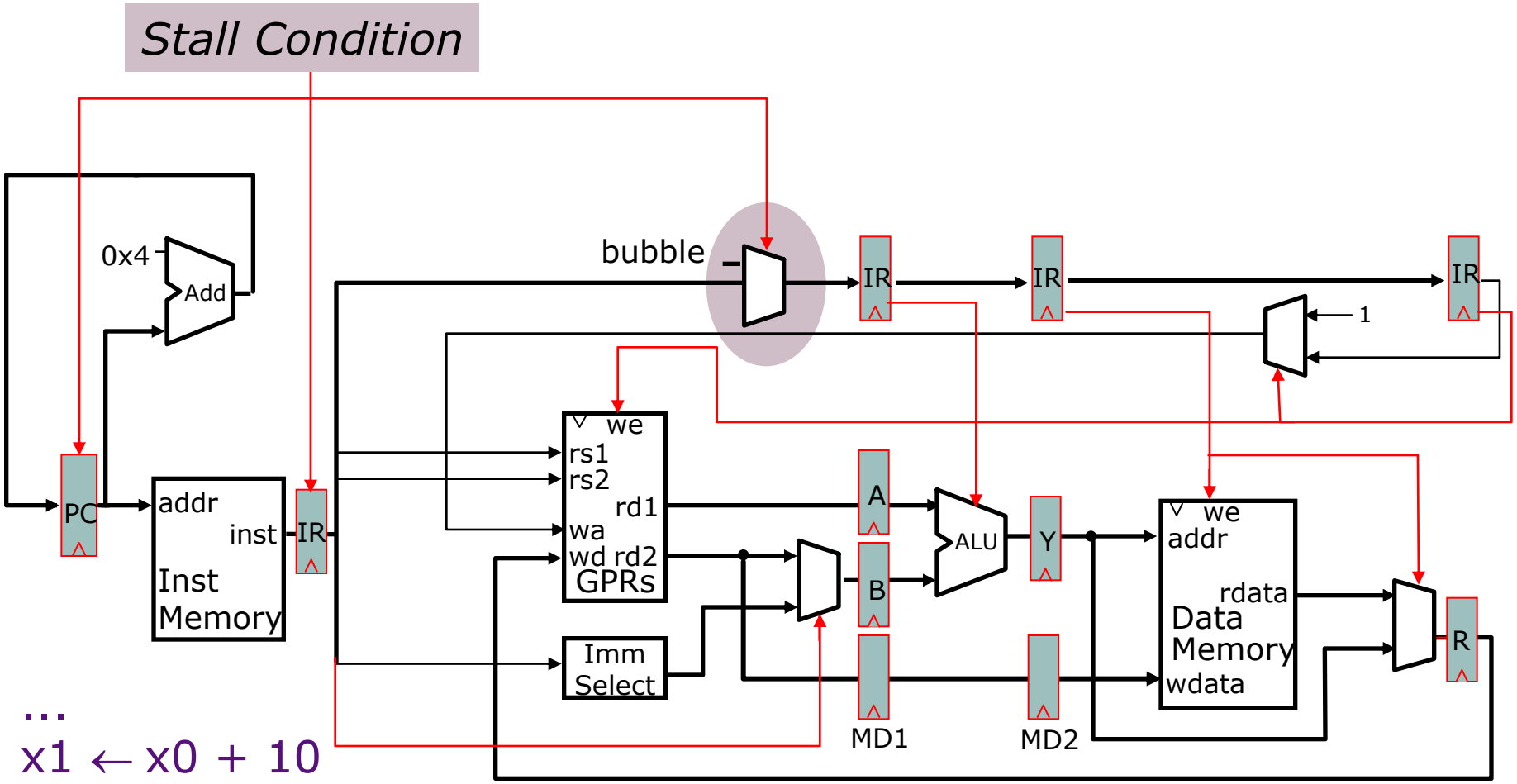
Feedback to Resolve Hazards



- Later stages provide dependence information to earlier stages which can *stall (or kill) instructions*

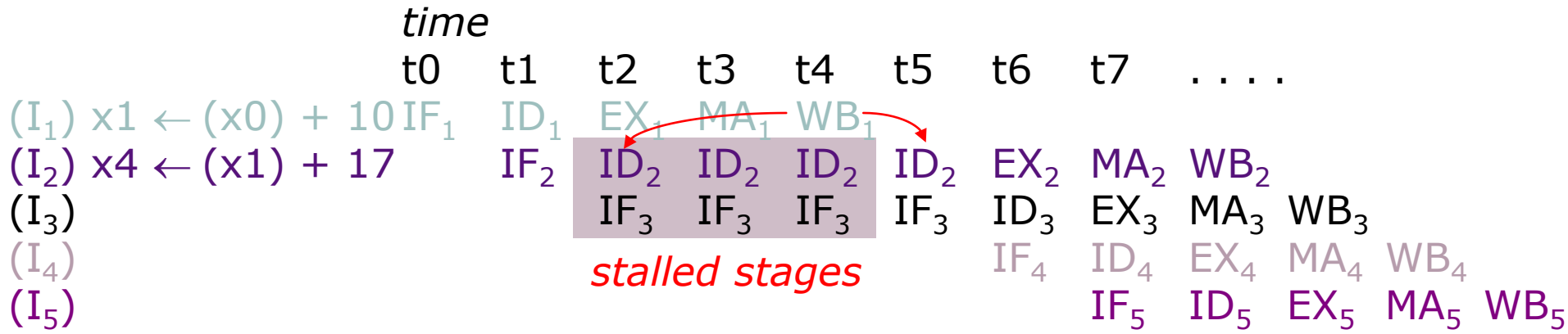
- Controlling a pipeline in this manner works provided *the instruction at stage i+1 can complete without any interference from instructions in stages 1 to i*
  (otherwise deadlocks may occur)

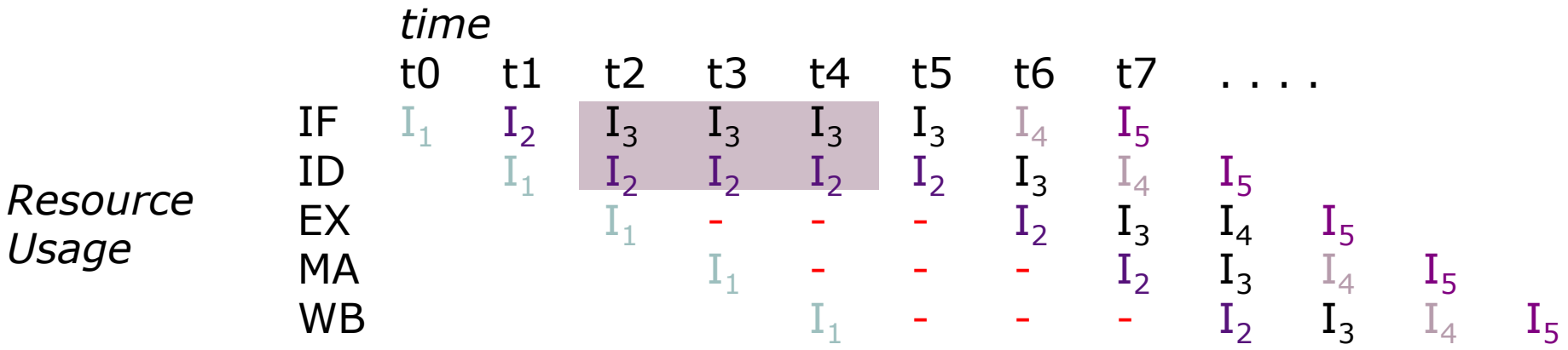
Interlocks to resolve Data Hazards



...
x1 ← x0 + 10
x4 ← x1 + 17
...

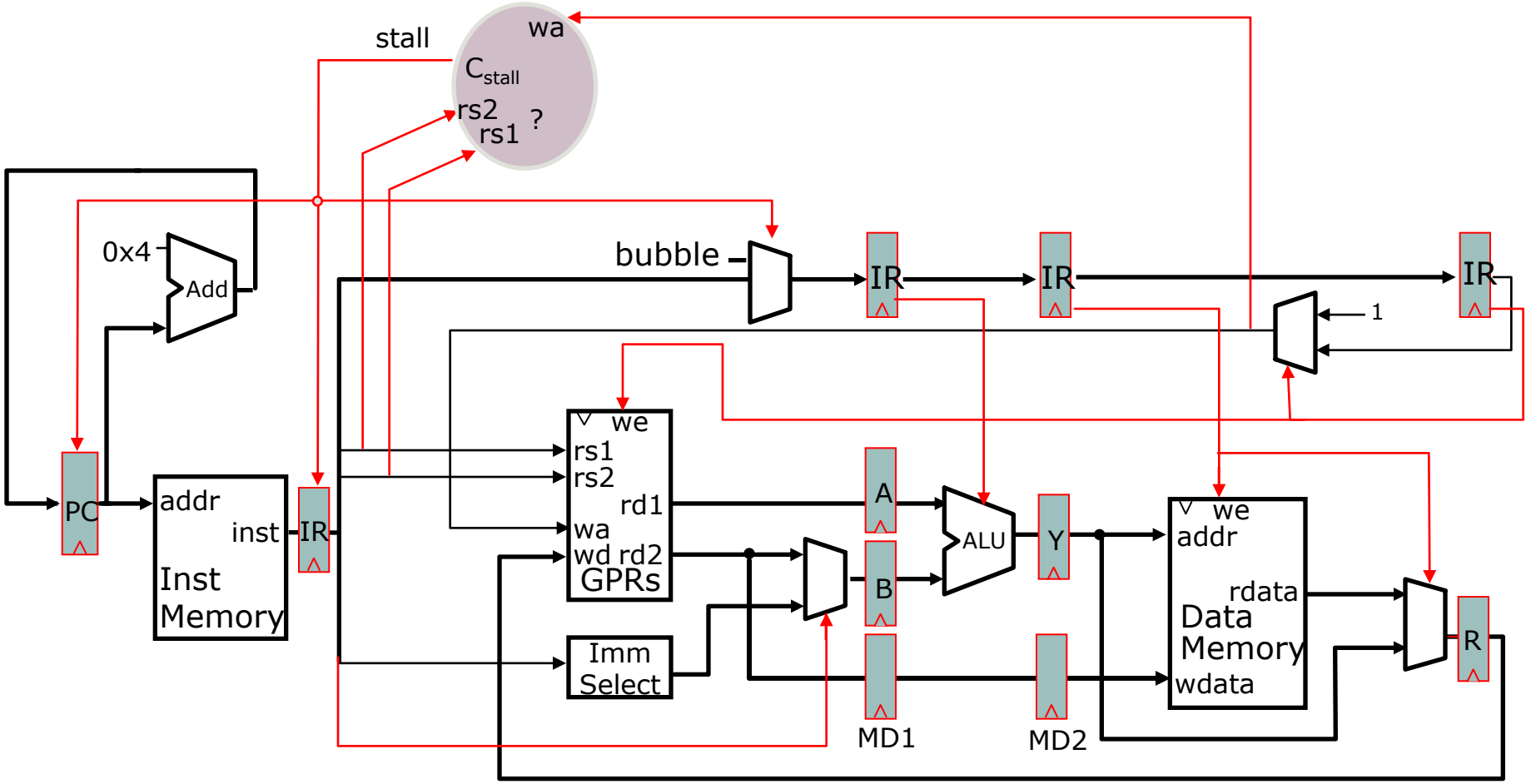
Stalled Stages and Pipeline Bubbles





- ⇒ *pipeline bubble*

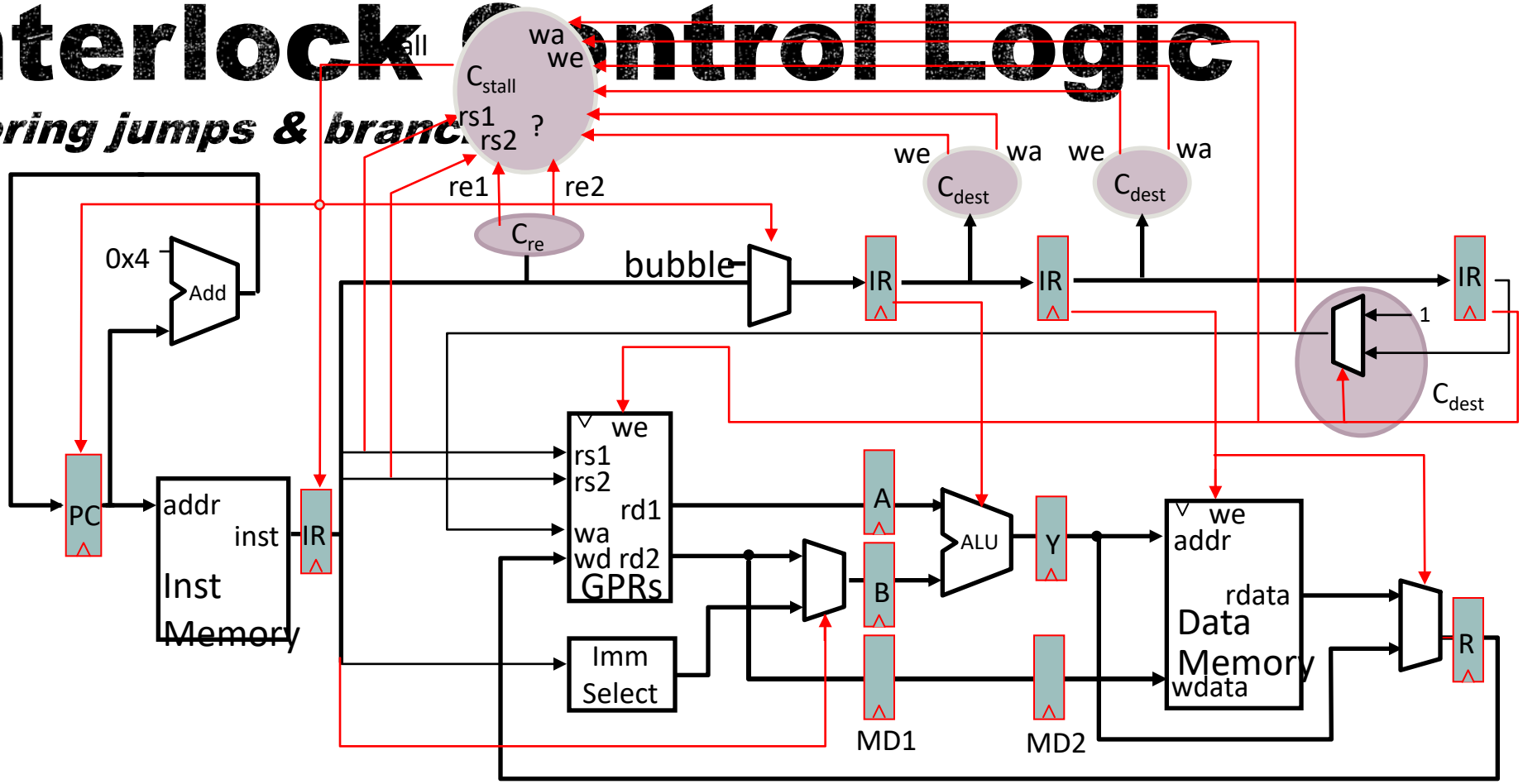
Interlock Control Logic



Compare the *source registers* of the instruction in the decode stage with the *destination register* of the *uncommitted* instructions.

Interlock Control Logic

ignoring jumps & branches

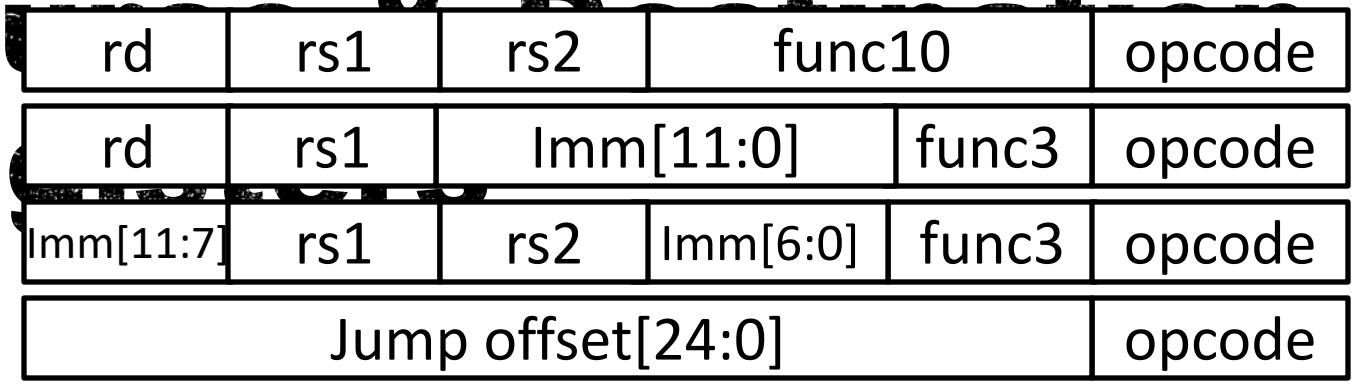


Should we always stall if an rs field matches some rd?

not every instruction writes a register ⇒ we

not every instruction reads a register ⇒ re

Sou Re



		source(s)	*destination*
ALU	rd ?? rs1 func10 rs2	rs1, rs2	rd
ALUI	rd ?? rs1 op imm	rs1	rd
LW	rd ??M [rs1 + imm]	rs1	rd
SW	M [rs1 + imm] ?? rs2	rs1, rs2	-
B*cond*	rs1,rs2	rs1, rs2	-
	true: PC ?? PC + imm		
	false: PC ?? PC + 4		
J	PC ?? PC + imm	-	-
JAL	x1 ?? PC, PC ?? PC + imm	-	x1
JALR	rd ?? PC, PC ?? rs1 + imm	rs1	rd

Deriving the Stall Signal

C_{dest}

ws = *Case* opcode

JAL □□X1

else □□rd

we = *Case* opcode

ALU, ALUi, LW,JALR □(ws □ 0)

JAL □□on

... □□off

C_{re}

re1 = *Case* opcode

ALU, ALUi,

LW, SW, Bcond, □□on

JALR

J, JAL □□off

re2 = *Case* opcode

ALU, SW, Bcond □□on

... □□off

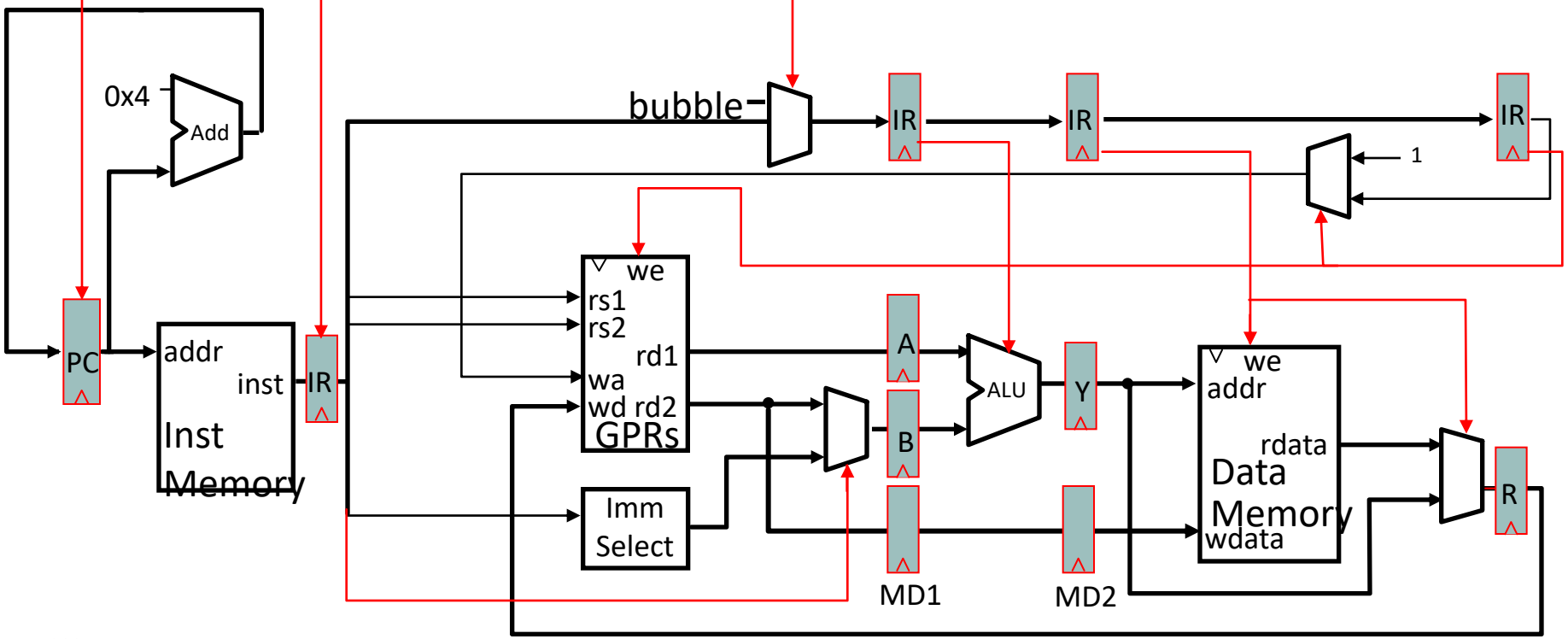
C_{stall} $stall = ((rs1_D = ws_E).we_E + (rs1_D = ws_M).we_M + (rs1_D = ws_W).we_W) . re1_D + ((rs2_D = ws_E).we_E + (rs2_D = ws_M).we_M + (rs2_D = ws_W).we_W) . re2_D$

This is not the full story !

Hazards due to Loads & Stores

Stall Condition

What if
x1+7 = x3+5 ?



...
M[x1+7] ← x2
x4 ← M[x3+5]
...

Is there any possible data hazard in this instruction sequence?

Load & Store Hazards

```
...
M[x1+7] ← x2
x4 ← M[x3+5]
...
```

x1+7 = x3+5 → *data hazard*

However, the hazard is avoided because *our memory system completes writes in one cycle !*

Load/Store hazards are sometimes resolved in the pipeline and sometimes in the memory system itself.

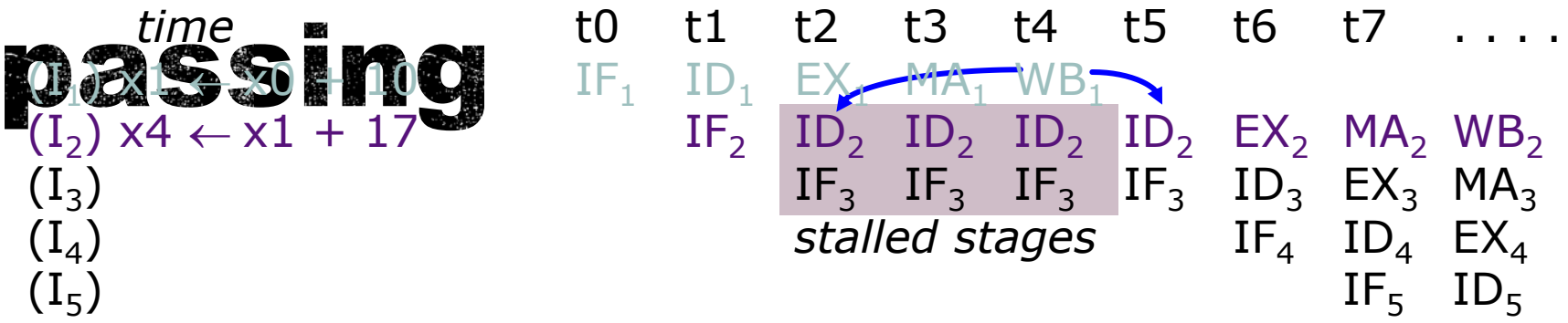
More on this later in the course.

Resolving Data Hazards (2)

Strategy 2:

Route data as soon as possible after it is calculated to the earlier pipeline stage → *bypass*

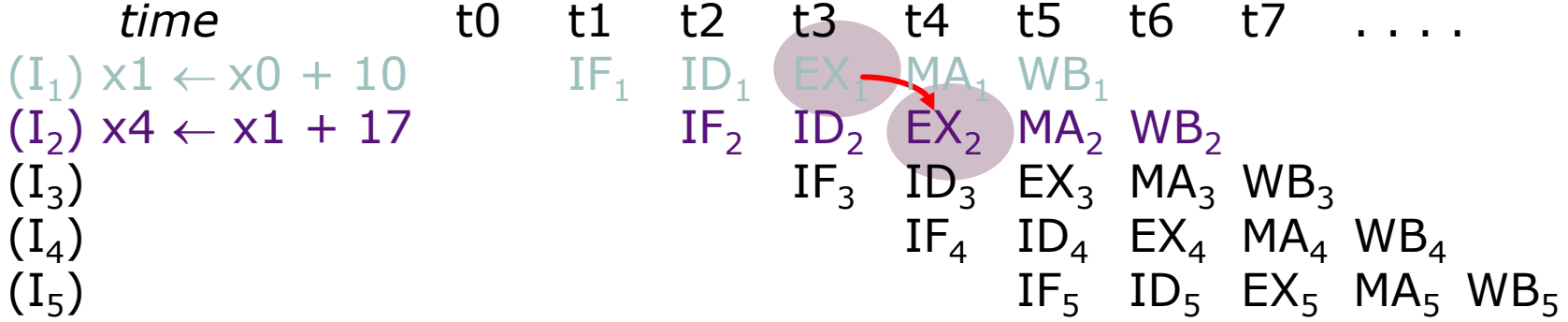
Bypassing



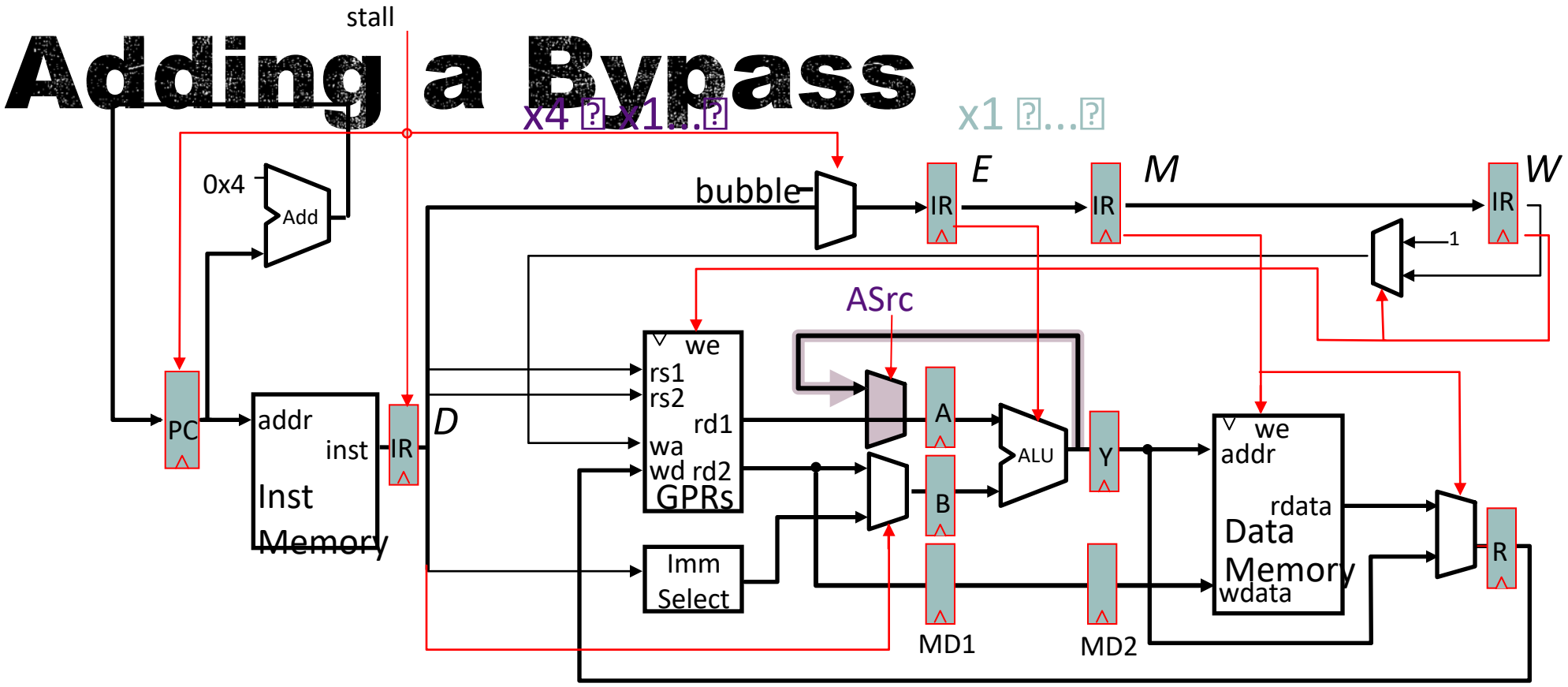
Each *stall or kill* introduces a bubble in the pipeline

□ □□*CPI > 1*

A new datapath, i.e., *a bypass*, can get the data from the output of the ALU to its input



Adding a Bypass



When does <u>this</u> bypass help?

...

(I_1) x1 ??x0 + 10	x1 ??M[x0 + 10]	JAL 500
(I_2) x4 ??x1 + 17	x4 ??x1 + 17	x4 ??x1 + 17
yes	*no*	*no*

The Bypass Signal

Deriving It from the Stall Signal

$$stall = (((rs1_D = ws_E).we_E + (rs1_D = ws_M).we_M + (rs1_D = ws_W).we_W).re1_D + ((rs2_D = ws_E).we_E + (rs2_D = ws_M).we_M + (rs2_D = ws_W).we_W).re2_D)$$

ws = *Case* opcode
JAL ??X1
else ??rd

we = *Case* opcode
ALU, ALUi, LW, JALR ?(ws ? 0)
JAL ??on
... ??off

$$ASrc = (rs1_D = ws_E).we_E.re1_D$$

Is this correct?

No because only ALU and ALUi instructions can benefit from this bypass

Split we_E into two components: we-bypass, we-stall

Bypass and Stall Signals

Split we_E into two components: we-bypass, we-stall

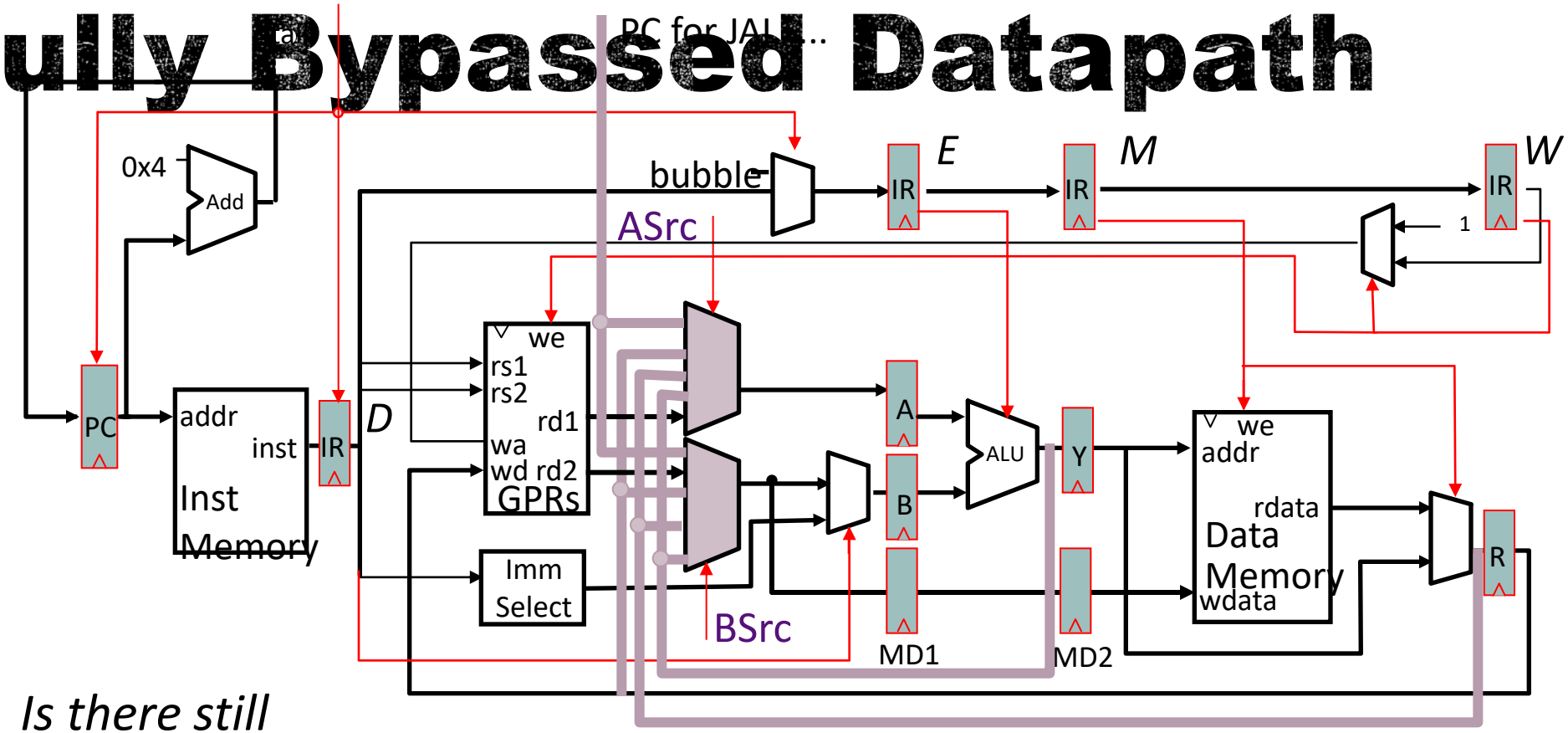
$we\text{-}bypass_E$ = *Case* $opcode_E$
ALU, ALUi → (ws ≠ 0)
... → off

$we\text{-}stall_E$ = *Case* $opcode_E$
LW, JALR → (ws ≠ 0)
JAL → on
... → off

$ASrc = (rs1_D = ws_E).we\text{-}bypass_E \,.\, re1_D$

$stall = ((rs1_D = ws_E).we\text{-}stall_E +$
$(rs1_D = ws_M).we_M + (rs1_D = ws_W).we_W).\, re1_D$
$+((rs2_D = ws_E).we_E + (rs2_D = ws_M).we_M + (rs2_D = ws_W).we_W).\, re2_D$

Fully Bypassed Datapath

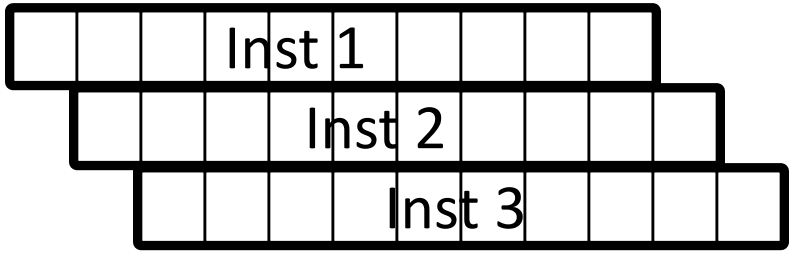


Is there still a need for the stall signal ?

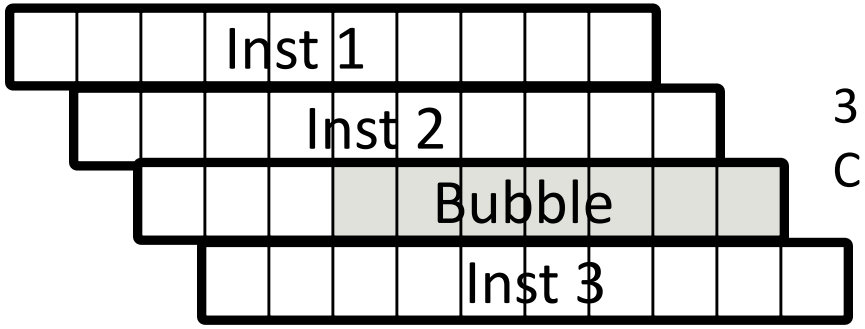
$$stall = (rs1_D = ws_E).(opcode_E = LW_E).(ws_E \neq 0).re1_D + (rs2_D = ws_E).(opcode_E = LW_E).(ws_E \neq 0).re2_D$$

Pipeline CPI Examples

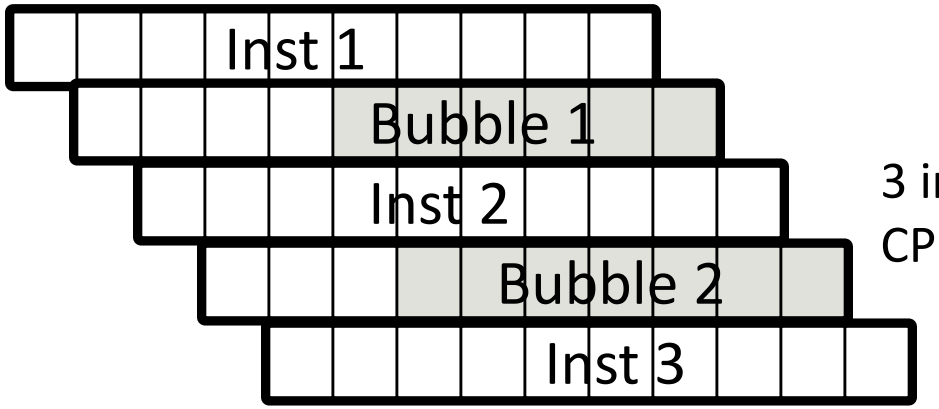
Measure from when first instruction finishes to when instruction sequence finishes.



3 instructions finish in 3 cycles
CPI = 3/3 =1



3 instructions finish in 4 cycles
CPI = 4/3 = 1.33



3 instructions finish in 5cycles
CPI = 5/3 = 1.67

Resolving Data Hazards (3)

Strategy 3: Speculate on the dependence!

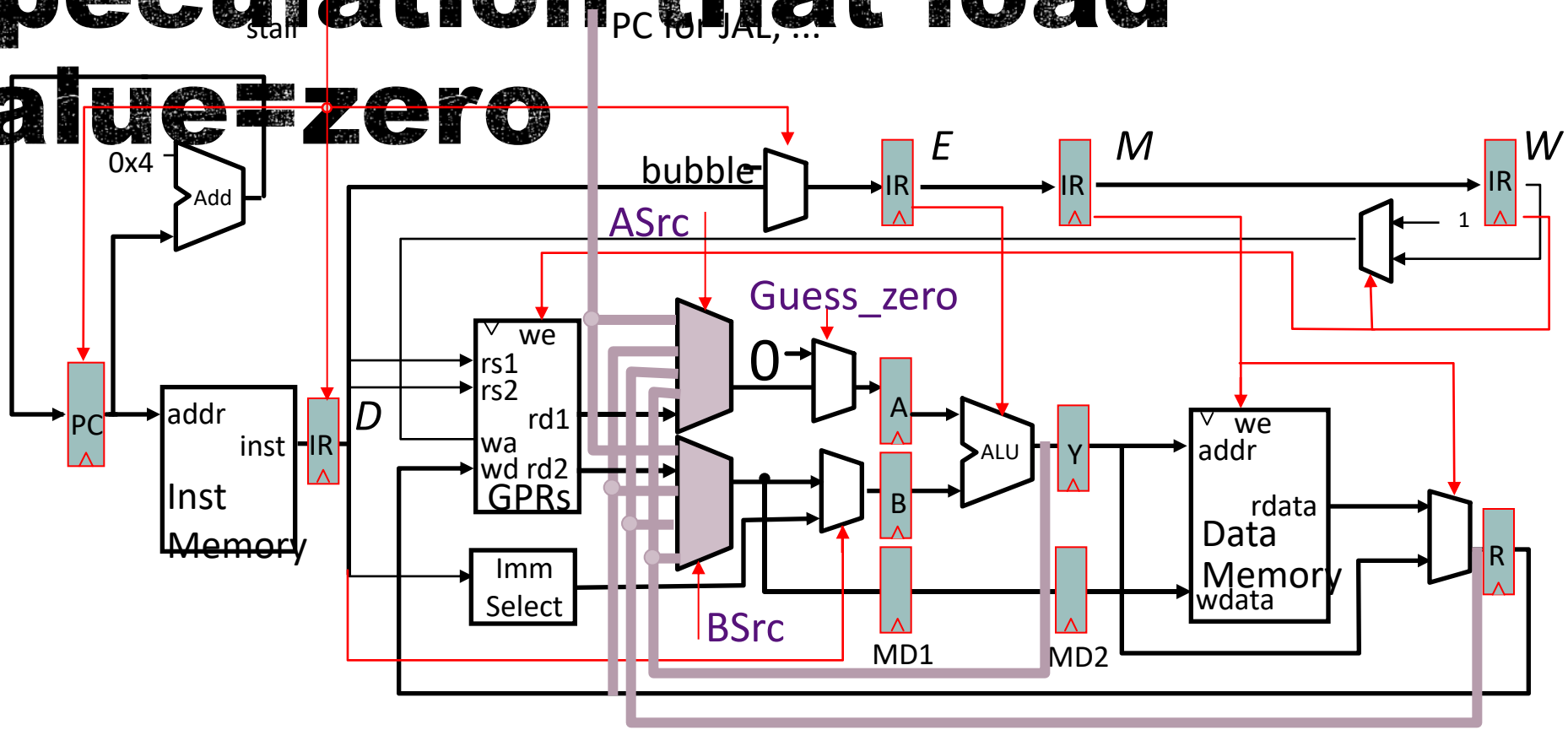
Two cases:

Guessed correctly ➔ do nothing

Guessed incorrectly ➔ kill and restart

…. We'll later see examples of this approach in more complex processors.

Speculation that load value=zero



$Guess\_zero = (rs1_D = ws_E).(opcode_E = LW_E).(ws_E \neq 0).re1_D$

Also need to add circuitry to remember that this was a guess and flush pipeline if load not zero!

Not worth doing in practice – why?

Control Hazards

What do we need to calculate next PC?

- For Jumps
  - Opcode, PC and offset
- For Jump Register
  - Opcode, Register value, and PC
- For Conditional Branches
  - Opcode, Register (for condition), PC and offset
- For all other instructions
  - Opcode and PC (and have to know it’s not one of above)

PC Calculation Bubbles

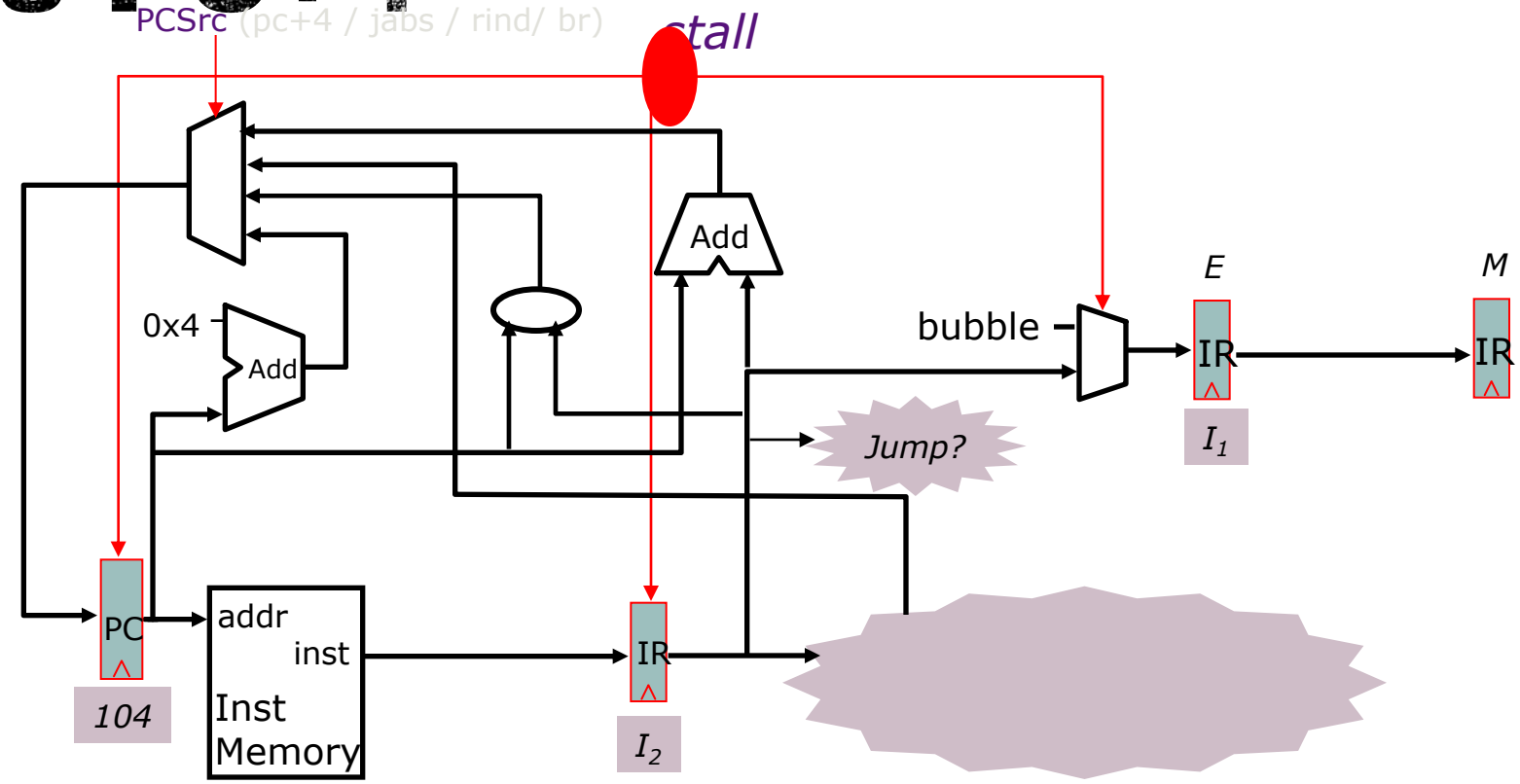
	time t0	t1	t2	t3	t4	t5	t6	t7	. . . .		
(I_1) x1 ← x0 + 10	IF_1	ID_1	EX_1	MA_1	WB_1						
(I_2) x3 ← x2 + 17		IF_2	IF_2	ID_2	EX_2	MA_2	WB_2				
(I_3)				IF_3	IF_3	ID_3	EX_3	MA_3	WB_3		
(I_4)						IF_4	IF_4	ID_4	EX_4	MA_4	WB_4

Resource Usage

	time t0	t1	t2	t3	t4	t5	t6	t7	. . . .		
IF	I_1	-	I_2	-	I_3	-	I_4				
ID		I_1	-	I_2	-	I_3	-	I_4			
EX			I_1	-	I_2	-	I_3	-	I_4		
MA				I_1	-	I_2	-	I_3	-	I_4	
WB					I_1	-	I_2	-	I_3	-	I_4

- ⇒ *pipeline bubble*

Speculate next address is PC+4

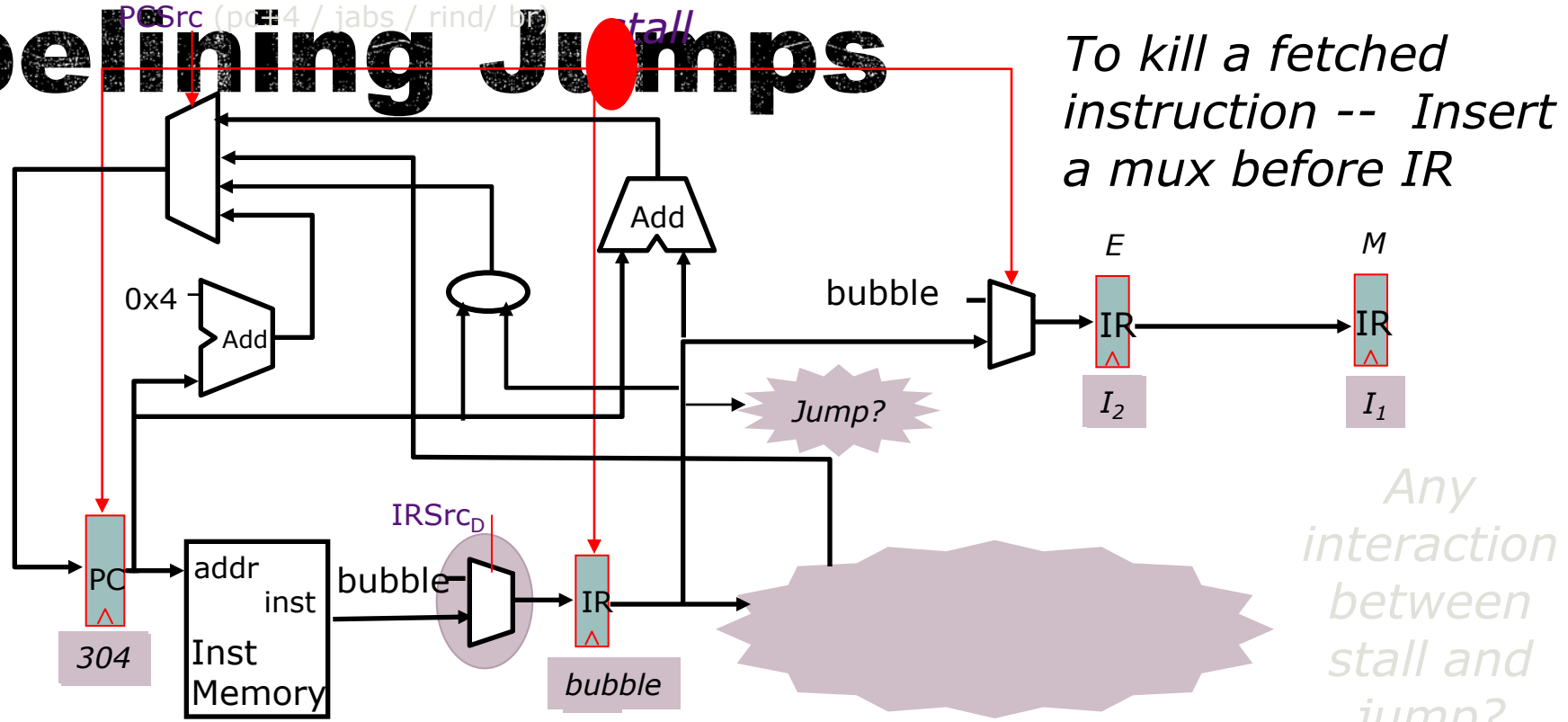


I_1 096 ADD
I_2 100 J 304
I_3 ~~104 ADD~~ *kill*
I_4 304 ADD

A jump instruction kills (not stalls) the following instruction

How?

Pipelining Jumps



To kill a fetched instruction -- Insert a mux before IR

Any interaction between stall and jump?

I_1 096 ADD
I_2 100 J 304
I_3 104 ~~ADD~~ *kill*
I_4 304 ADD

$IRSrc_D$ = *Case* $opcode_D$
J, JAL ⇒ bubble
... ⇒ IM

Jump Pipeline Diagrams

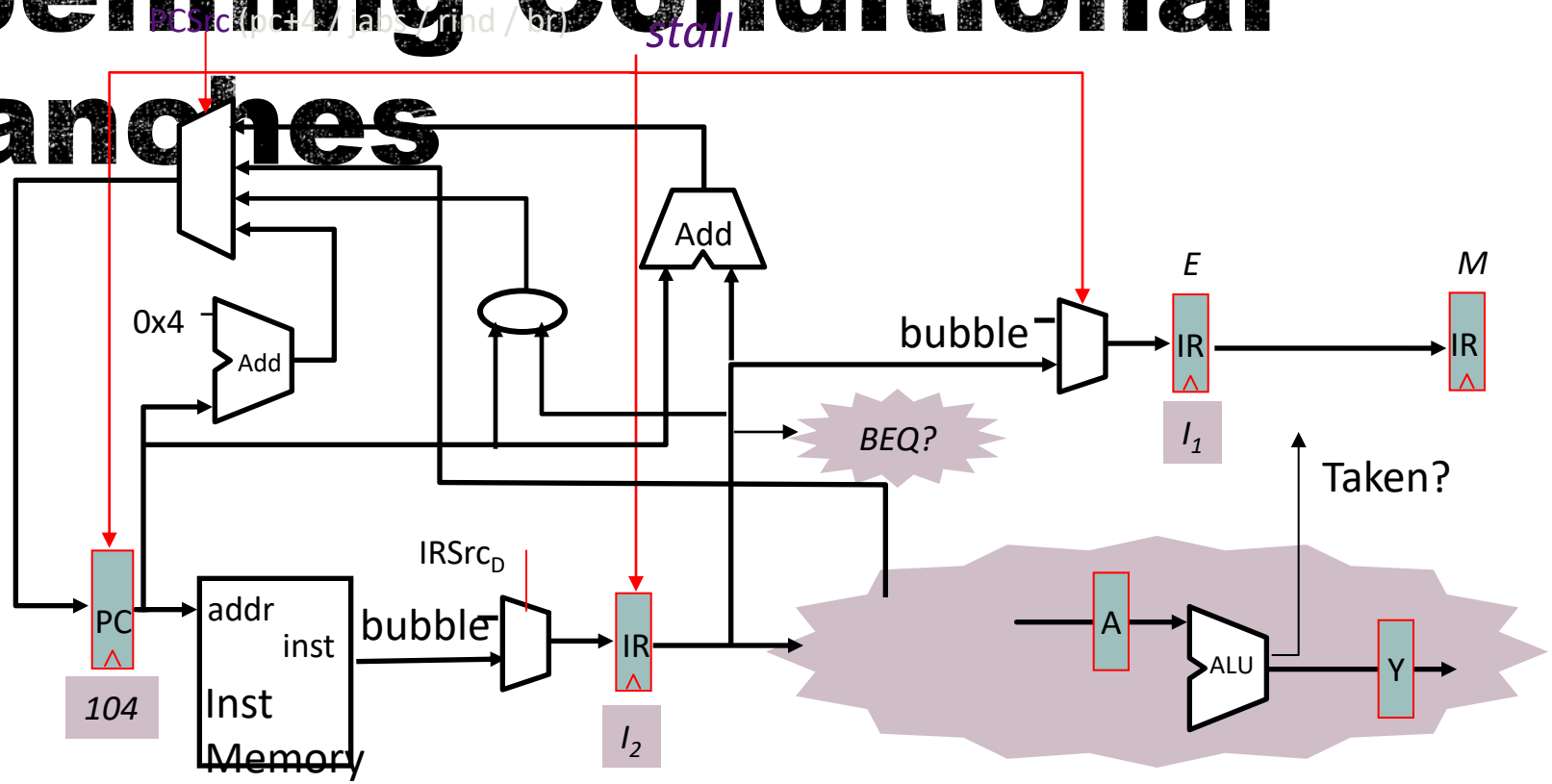
	time t0	t1	t2	t3	t4	t5	t6	t7
(I_1) 096: ADD	IF_1	ID_1	EX_1	MA_1	WB_1			
(I_2) 100: J 304		IF_2	ID_2	EX_2	MA_2	WB_2		
(I_3) 104: ADD			IF_3	-	-	-	-	
(I_4) 304: ADD				IF_4	ID_4	EX_4	MA_4	WB_4

Resource Usage

	time t0	t1	t2	t3	t4	t5	t6	t7	. . . .
IF	I_1	I_2	I_3	I_4	I_5				
ID		I_1	I_2	-	I_4	I_5			
EX			I_1	I_2	-	I_4	I_5		
MA				I_1	I_2	-	I_4	I_5	
WB					I_1	I_2	-	I_4	I_5

- $\Rightarrow$ *pipeline bubble*

Pipelining Conditional Branches

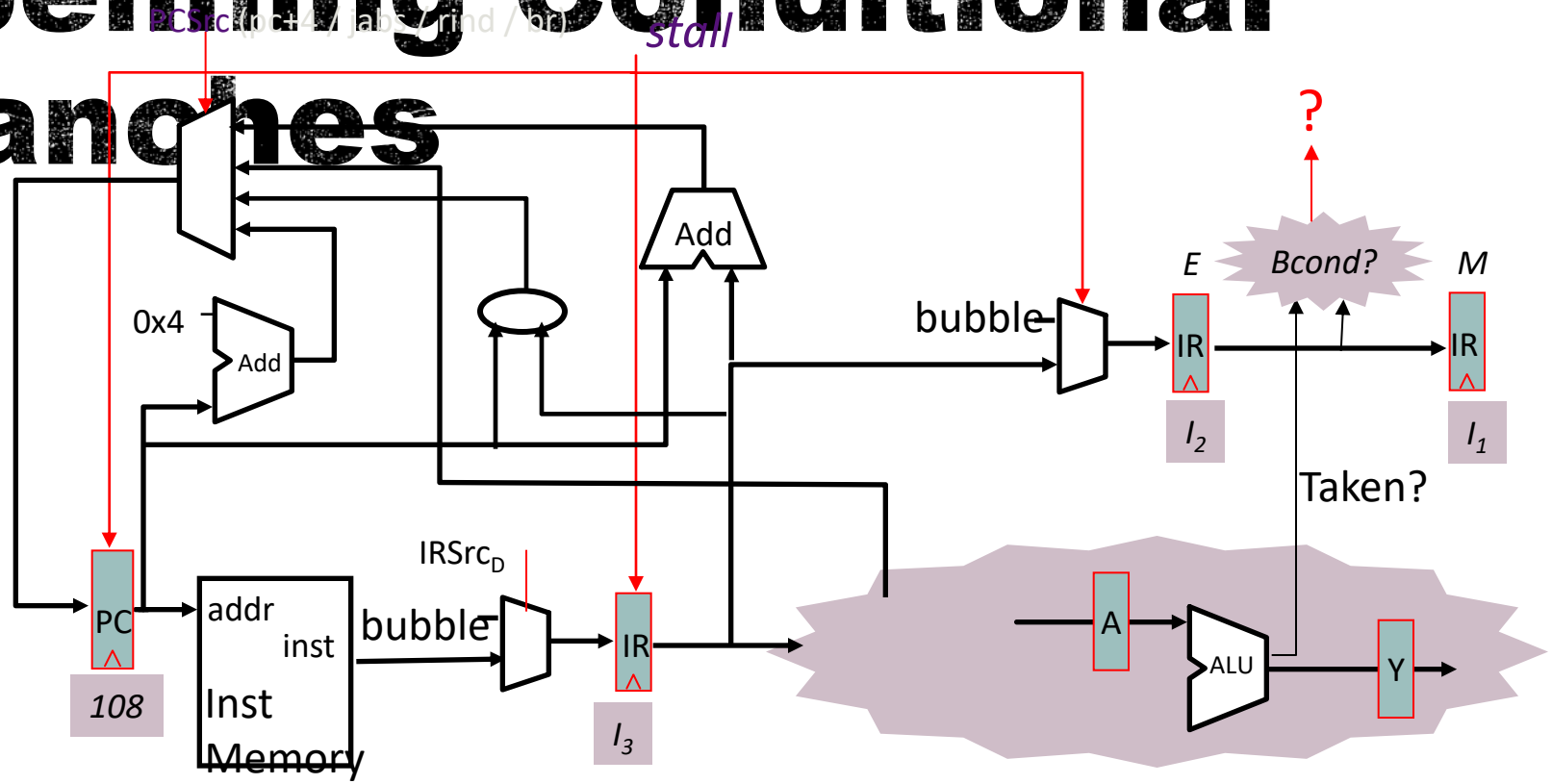


I_1 096 ADD
I_2 100 BEQ x1,x2 +200
I_3 104 ADD
I_4 304 ADD

Branch condition is not known until the execute stage

what action should be taken in the decode stage ?

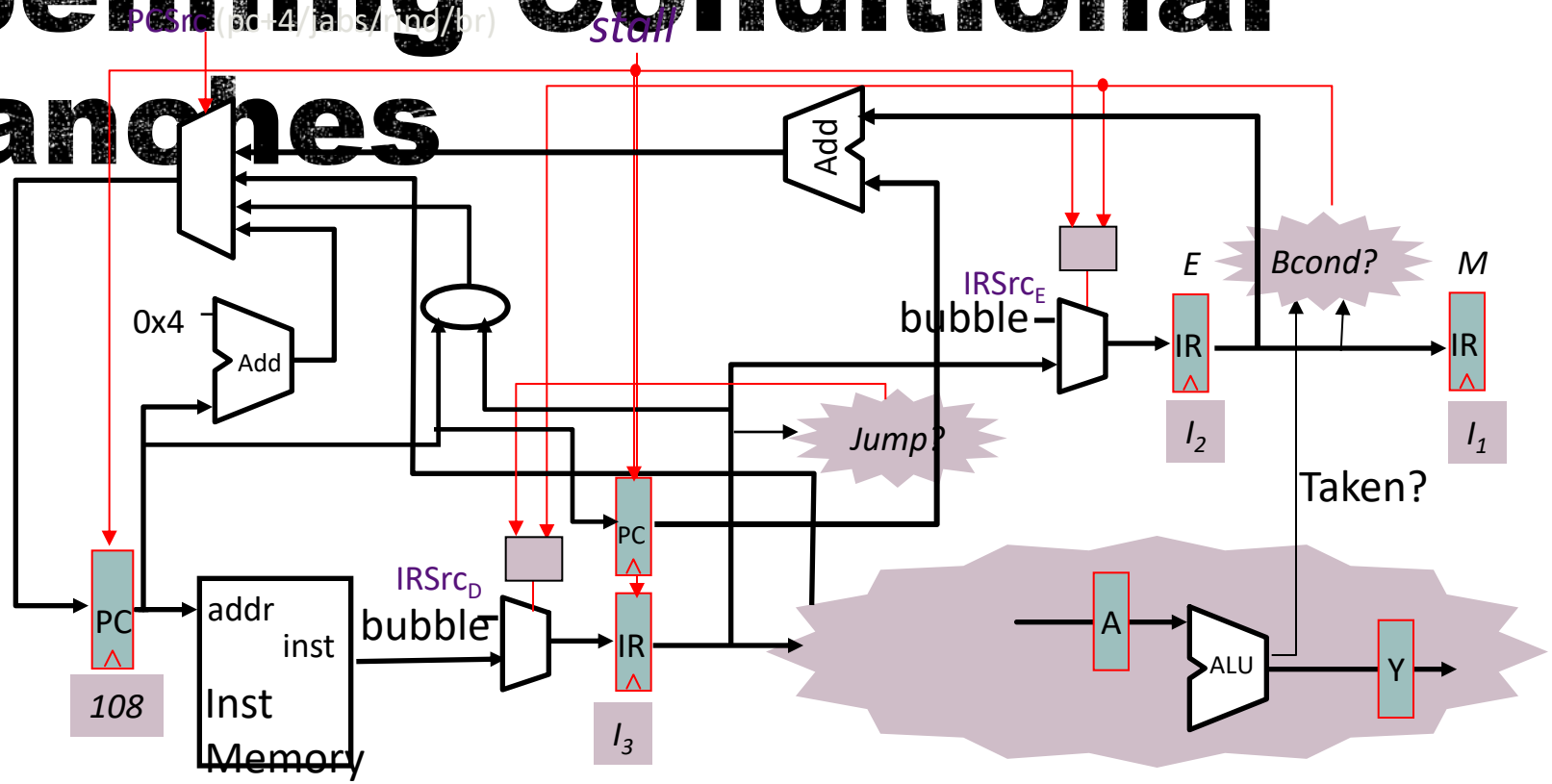
Pipelining Conditional Branches



I_1 096 ADD
I_2 100 BEQ x1,x2 +200
I_3 104 ADD
I_4 304 ADD

If the branch is taken
- kill the two following instructions
- the instruction at the decode stage is not valid ⇒ *stall signal is not valid*

Pipelining Conditional Branches



$I_{1:}$ 096 ADD
$I_{2:}$ 100 BEQ x1,x2 +200
$I_{3:}$ 104 ADD
$I_{4:}$ 304 ADD

If the branch is taken
- kill the two following instructions
- the instruction at the decode stage is not valid ⇒ *stall signal is not valid*

Branch Pipeline Diagrams

(resolved in execute stage)

	time t0	t1	t2	t3	t4	t5	t6	t7	. . . .
(I_1) 096: ADD	IF_1	ID_1	EX_1	MA_1	WB_1				
(I_2) 100: BEQ +200		IF_2	ID_2	EX_2	MA_2	WB_2			
(I_3) 104: ADD			IF_3	ID_3	-	-	-		
(I_4) 108:				IF_4	-	-	-	-	
(I_5) 304: ADD					IF_5	ID_5	EX_5	MA_5	WB_5

Resource Usage

	time t0	t1	t2	t3	t4	t5	t6	t7	. . . .
IF	I_1	I_2	I_3	I_4	I_5				
ID		I_1	I_2	I_3	-	I_5			
EX			I_1	I_2	-	-	I_5		
MA				I_1	I_2	-	-	I_5	
WB					I_1	I_2	-	-	I_5

- ⇒ *pipeline bubble*

Acknowledgements

- These slides contain material developed and copyright by:
  - Arvind (MIT)
  - Krste Asanovic (MIT/UCB)
  - Joel Emer (Intel/MIT)
  - James Hoe (CMU)
  - John Kubiatowicz (UCB)
  - David Patterson (UCB)

- MIT material derived from course 6.823
- UCB material derived from course CS252